
DATALINES ;
NO 2 YES 8
RUN ;
PROC FREQ DATA $=$ FINAL ; WEIGHT $N$;
TABLES CURE / BINOMIAL ; EXACT BINOMIAL ; RUN ;

| CURE | Frequency | Percent | Cumulative <br> Frequency | Cumulative <br> Percent |
| :--- | :--- | :--- | :--- | :--- |
| NO | 2 | 20.00 | 2 | 20.00 |
| YES | 8 | 80.00 | 10 | 100.00 |

Binomial Proportion

For CURE $=$ NO the Proportion ( P ) is 0.2000 with a Sample Size of 10

## RESULTS FROM SAS FREQ PROCEDURE (continued)

Binomial Proportion

| CURE $=$ NO |  |
| :--- | :--- |
| Proportion $(P)$ | 0.2000 |
| ASE | 0.1265 |

95\% Lower Conf Limit 0.0000
95\% Upper Conf Limit 0.4479

Exact Conf Limits
95\% Lower Conf Limit 0.0252
95\% Upper Conf Limit 0.5561

| Test of $\mathrm{HO}:$ Proportion $=0.5$ |  |
| :--- | :--- |
| ASE under H0 | 0.1581 |
| Z | -1.8974 |
| One-sided $\mathrm{Pr}<\mathrm{Z}$ | 0.0289 |
| Two-sided $\mathrm{Pr}>\|\mathrm{Z}\|$ | 0.0578 |
|  |  |
| Exact Test |  |
| One-sided $\mathrm{Pr}<=\mathrm{P}$ | 0.0547 |
| Two-sided $=2$ * One-sided | 0.1094 |

## [ ASE = Asymptotic standard error ]

MY NOTE: Because p value is greater than $0.0595 \% \mathrm{Cl}$ contains $\mathrm{P}=0.50$

TBAW

A popular measure of the size of the variability expected between sample proportions repeatedly selected from a population is called the standard error.

Standard Error(SE) of a Sample Proportion p

$$
S E=\sqrt{\frac{p \times q}{n}}=\sqrt{\frac{p \times(1-p)}{n}} \quad p=0.8
$$

Standard Error of a Sample Proportion under the Assumption that the Probability of Success is $P$


In the previous output from the FREQ procedure the standard error of a proportion was reported twice.

First, for the observed proportion $\mathrm{p}=0.2$ and next for the proportion expected under the Null Hypothesis $\mathrm{P}=0.50$. In both cases $\mathrm{n}=10$.

$$
\begin{aligned}
& \text { Standard Error of Proportion }(2 / 10)=0.2 \\
& S E=\sqrt{\frac{0.2 \times 0.8}{10}}=0.1265 \\
& \text { Standard Error of Probability } 0.5 \text { for } n=10 \\
& S E=\sqrt{\frac{0.5 \times 0.5}{10}}=0.1581
\end{aligned}
$$

Exact Conf Limits 95\% Lower Conf Limit 0.0252 95\% Upper Conf Limit 0.5561

Test of H0: Proportion = 0.5
Exact Test One-sided $\mathrm{Pr}<=\mathrm{P}$
0.0547

Two-sided $=2$ * One-sided
0.1094

MY NOTE: The 2-Tail $p$ value $=0.1094$ and the $95 \%$ confidence interval does contain 0.5.
The Null Hypothesis $\left(\mathrm{H}_{0}\right)$ is that $\mathrm{P}_{\text {но }}=0.50$

DATA FINAL ; INPUT CURE \$ N @@ ;
DATALINES ;
NO 1 YES 9
RUN ;

PROC FREQ DATA = FINAL ; WEIGHT N ;
TABLES CURE / BINOMIAL ; EXACT BINOMIAL ; RUN ;

| CURE | Frequency | Percent | Cumulative <br> Frequency | Cumulative <br> Percent |
| :--- | :--- | :--- | :--- | :--- |
| NO | 1 | $* * 10.00$ | 1 | 10.00 |
| YES | 9 | 90.00 | 10 | 100.00 |

** Scientist discovered an error and made the correction !

Exact Conf Limits 95\% Lower Conf Limit 0.0025 95\% Upper Conf Limit 0.4450

Test of $\mathrm{H}_{0}$ : Proportion $=0.5$
Exact Test One-sided $\mathrm{Pr}<=\mathrm{P} \quad 0.0107$
Two-sided = 2 * One-sided 0.0214

MY NOTE: The 2 -Tail $p$ value $=0.0215$ and the $95 \%$ confidence interval does NOT contain $\mathrm{P}_{\text {но }}=0.5$

## CONCLUSION

If this result is due to chance the probability of getting 9 or more successes for the new drug is 0.0107 and the probability of getting one or fewer successes is also 0.0107

The 2 -tail p value 0.0214 is the probability of getting a result as extreme or more extreme than the observed difference under the Null Hypothesis that the difference was due to chance, that is, $\mathrm{P}=0.5$

## CONCLUSION (con’t)

We would report that 90 percent of the patients cured on the new drug is SIGNIFICANTLY greater than the null hypothesized proportion of 0.5 .
( $\mathrm{p}=0.0214$ and $95 \% \mathrm{Cl}=0.0025,0.4450$ )

NOTE: 95\% confidence interval CI does NOT contain the Hypothetical Probability P = 0.5

## End of Lecture 1

Next up in Part 1 Lecture 2: The Central Limit Theorem

